

# EXEMPLAR SOLUTIONS MATHS

Class  
**11**



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## Chapter 2- Relations and functions

### EXERCISE

#### SHORT ANSWER TYPE

1. Let  $A = \{-1, 2, 3\}$  and  $B = \{1, 3\}$ . Determine

(i)  $A \times B$

(ii)  $B \times A$

(iii)  $B \times B$

(iv)  $A \times A$

**Solution:**

According to the question,

$A = \{-1, 2, 3\}$  and  $B = \{1, 3\}$

(i)  $A \times B$

$\{-1, 2, 3\} \times \{1, 3\}$

So,  $A \times B = \{(-1, 1), (-1, 3), (2, 1), (2, 3), (3, 1), (3, 3)\}$

Hence, the Cartesian product =  $\{(-1, 1), (-1, 3), (2, 1), (2, 3), (3, 1), (3, 3)\}$

(ii)  $B \times A$ .

$\{1, 3\} \times \{-1, 2, 3\}$

So,  $B \times A = \{(1, -1), (1, 2), (1, 3), (3, -1), (3, 2), (3, 3)\}$

Hence, the Cartesian product =  $\{(1, -1), (1, 2), (1, 3), (3, -1), (3, 2), (3, 3)\}$

(iii)  $B \times B$

$\{1, 3\} \times \{1, 3\}$

So,  $B \times B = \{(1, 1), (1, 3), (3, 1), (3, 3)\}$

Hence, the Cartesian product =  $\{(1, 1), (1, 3), (3, 1), (3, 3)\}$

(iv)  $A \times A$

$\{-1, 2, 3\} \times \{-1, 2, 3\}$

So,  $A \times A = \{(-1, -1), (-1, 2), (-1, 3), (2, -1), (2, 2), (2, 3), (3, -1), (3, 2), (3, 3)\}$

Hence,

the Cartesian product =  $\{(-1, -1), (-1, 2), (-1, 3), (2, -1), (2, 2), (2, 3), (3, -1), (3, 2), (3, 3)\}$

2. If  $P = \{x : x < 3, x \in \mathbb{N}\}$ ,  $Q = \{x : x \leq 2, x \in \mathbb{W}\}$ . Find  $(P \cup Q) \times (P \cap Q)$ , where  $\mathbb{W}$  is the set of whole numbers.

**Solution:**

According to the question,

$P = \{x : x < 3, x \in \mathbb{N}\}$ ,  $Q = \{x : x \leq 2, x \in \mathbb{W}\}$  where  $\mathbb{W}$  is the set of whole numbers

$P = \{1, 2\}$

$Q = \{0, 1, 2\}$

Now

$(P \cup Q) = \{1, 2\} \cup \{0, 1, 2\} = \{0, 1, 2\}$

And,

$(P \cap Q) = \{1, 2\} \cap \{0, 1, 2\} = \{1, 2\}$

We need to find the Cartesian product of  $(P \cup Q) = \{0, 1, 2\}$  and  $(P \cap Q) = \{1, 2\}$

So,

$(P \cup Q) \times (P \cap Q) = \{0, 1, 2\} \times \{1, 2\}$

$= \{(0, 1), (0, 2), (1, 1), (1, 2), (2, 1), (2, 2)\}$

Hence, the Cartesian product =  $\{(0, 1), (0, 2), (1, 1), (1, 2), (2, 1), (2, 2)\}$



**3. If  $A = \{x : x \in W, x < 2\}$ ,  $B = \{x : x \in N, 1 < x < 5\}$ ,  $C = \{3, 5\}$  find**

**(i)  $A \times (B \cap C)$**

**(ii)  $A \times (B \cup C)$**

**Solution:**

According to the question,

$A = \{x : x \in W, x < 2\}$ ,  $B = \{x : x \in N, 1 < x < 5\}$   $C = \{3, 5\}$ ;  $W$  is the set of whole numbers

$A = \{x : x \in W, x < 2\} = \{0, 1\}$

$B = \{x : x \in N, 1 < x < 5\} = \{2, 3, 4\}$

(i)

$(B \cap C) = \{2, 3, 4\} \cap \{3, 5\}$

$(B \cap C) = \{3\}$

$A \times (B \cap C) = \{0, 1\} \times \{3\} = \{(0, 3), (1, 3)\}$

Hence, the Cartesian product =  $\{(0, 3), (1, 3)\}$

(ii)

$(B \cup C) = \{2, 3, 4\} \cup \{3, 5\}$

$(B \cup C) = \{2, 3, 4, 5\}$

$A \times (B \cup C) = \{0, 1\} \times \{2, 3, 4, 5\} = \{(0, 2), (0, 3), (0, 4), (0, 5), (1, 2), (1, 3), (1, 4), (1, 5)\}$

Hence, the Cartesian product =  $\{(0, 2), (0, 3), (0, 4), (0, 5), (1, 2), (1, 3), (1, 4), (1, 5)\}$

**4. In each of the following cases, find a and b.**

**(i)  $(2a + b, a - b) = (8, 3)$**

**(ii)  $(a/4, a - 2b) = (0, 6 + b)$**

**Solution:**

(i)

According to the question,

$(2a + b, a - b) = (8, 3)$

Given the ordered pairs are equal, so corresponding elements will be equal.

Hence,

$2a + b = 8$  and  $a - b = 3$

Now  $a - b = 3$

$\Rightarrow a = 3 + b$

Substituting the value of a in the equation  $2a + b = 8$ ,

We get,

$2(3 + b) + b = 8$

$\Rightarrow 6 + 2b + b = 8$

$\Rightarrow 3b = 8 - 6 = 2$

$\Rightarrow b = 2/3$

Substituting the value of b in equation  $(a - b = 3)$ ,

We get,

$\Rightarrow a - 2/3 = 3$

$\Rightarrow a = 3 + 2/3$

$\Rightarrow a = (9 + 2)/3$

$\Rightarrow a = 11/3$

Hence the value of  $a = 11/3$  and  $b = 2/3$  respectively.

(ii)

According to the question,

$$\left(\frac{a}{4}, a - 2b\right) = (0, 6 + b)$$

Given the ordered pairs are equal, so corresponding elements will be equal.

$$a/4 = 0 \text{ and } a - 2b = 6 + b$$

$$\text{Now } a/4 = 0$$

$$\Rightarrow a = 0$$

Substituting the value of  $a$  in the equation  $(a - 2b = 6 + b)$ ,

We get,

$$0 - 2b = 6 + b$$

$$\Rightarrow -2b - b = 6$$

$$\Rightarrow -3b = 6$$

$$\Rightarrow b = -6/3$$

$$\Rightarrow b = -2$$

Hence, the value of  $a = 0$  and  $b = -2$  respectively

**5. Given  $A = \{1, 2, 3, 4, 5\}$ ,  $S = \{(x, y) : x \in A, y \in A\}$ . Find the ordered pairs which satisfy the conditions given below:**

**(i)  $x + y = 5$**

**(ii)  $x + y < 5$**

**(iii)  $x + y > 8$**

**Solution:**

According to the question,  $A = \{1, 2, 3, 4, 5\}$ ,  $S = \{(x, y) : x \in A, y \in A\}$

(i)  $x + y = 5$

So, we find the ordered pair such that  $x + y = 5$ , where  $x$  and  $y$  belongs to set  $A = \{1, 2, 3, 4, 5\}$ ,

$$1 + 1 = 2 \neq 5$$

$$1 + 2 = 3 \neq 5$$

$$1 + 3 = 4 \neq 5$$

$$1 + 4 = 5 \Rightarrow \text{the ordered pair is } (1, 4)$$

$$1 + 5 = 6 \neq 5$$

$$2 + 1 = 3 \neq 5$$

$$2 + 2 = 4 \neq 5$$

$$2 + 3 = 5 \Rightarrow \text{the ordered pair is } (2, 3)$$

$$2 + 4 = 6 \neq 5$$

$$2 + 5 = 7 \neq 5$$

$$3 + 1 = 4 \neq 5$$

$$3 + 2 = 5 \Rightarrow \text{the ordered pair is } (3, 2)$$

$$3 + 3 = 6 \neq 5$$

$$3 + 4 = 7 \neq 5$$

$$3 + 5 = 8 \neq 5$$

$$4 + 1 = 5 \Rightarrow \text{the ordered pair is } (4, 1)$$

$$4 + 2 = 6 \neq 5$$

$$4 + 3 = 7 \neq 5$$

$$4 + 4 = 8 \neq 5$$

$$4 + 5 = 9 \neq 5$$

$$5 + 1 = 6 \neq 5$$

$$5 + 2 = 7 \neq 5$$

$$5 + 3 = 8 \neq 5$$

$$5 + 4 = 9 \neq 5$$

$$5 + 5 = 10 \neq 5$$

Therefore, the set of ordered pairs satisfying  $x + y = 5 = \{(1,4), (2,3), (3,2), (4,1)\}$ .

(ii)  $x + y < 5$

So, we find the ordered pair such that  $x + y < 5$ , where  $x$  and  $y$  belongs to set  $A = \{1, 2, 3, 4, 5\}$

$$1 + 1 = 2 < 5 \Rightarrow \text{the ordered pairs is } (1, 1)$$

$$1 + 2 = 3 < 5 \Rightarrow \text{the ordered pairs is } (1, 2)$$

$$1 + 3 = 4 < 5 \Rightarrow \text{the ordered pairs is } (1, 3)$$

$$1 + 4 = 5$$

$$1 + 5 = 6 > 5$$

$$2 + 1 = 3 < 5 \Rightarrow \text{the ordered pairs is } (2, 1)$$

$$2 + 2 = 4 < 5 \Rightarrow \text{the ordered pairs is } (2, 2)$$

$$2 + 3 = 5$$

$$2 + 4 = 6 > 5$$

$$2 + 5 = 7 > 5$$

$$3 + 1 = 4 < 5 \Rightarrow \text{the ordered pairs is } (3, 1)$$

$$3 + 2 = 5$$

$$3 + 3 = 6 > 5$$

$$3 + 4 = 7 > 5$$

$$3 + 5 = 8 > 5$$

$$4 + 1 = 5$$

$$4 + 2 = 6 > 5$$

$$4 + 3 = 7 > 5$$

$$4 + 4 = 8 > 5$$

$$4 + 5 = 9 > 5$$

$$5 + 1 = 6 > 5$$

$$5 + 2 = 7 > 5$$

$$5 + 3 = 8 > 5$$

$$5 + 4 = 9 > 5$$

$$5 + 5 = 10 > 5$$

Therefore, the set of ordered pairs satisfying  $x + y < 5 = \{(1,1), (1,2), (1,3), (2, 1), (2,2), (3,1)\}$ .

(iii)  $x + y > 8$

So, we find the ordered pair such that  $x + y > 8$ , where  $x$  and  $y$  belongs to set  $A = \{1, 2, 3, 4, 5\}$

$$1 + 1 = 2 < 8$$

$$1 + 2 = 3 < 8$$

$$1 + 3 = 4 < 8$$

$$1 + 4 = 5 < 8$$

$$1 + 5 = 6 < 8$$

$$2 + 1 = 3 < 8$$

$$2 + 2 = 4 < 8$$

$$2 + 3 = 5 < 8$$

$$2 + 4 = 6 < 8$$

$$2 + 5 = 7 < 8$$

$$3 + 1 = 4 < 8$$

$$3 + 2 = 5 < 8$$

$$3 + 3 = 6 < 8$$

$$3 + 4 = 7 < 8$$

$$3 + 5 = 8$$

$$4 + 1 = < 8$$

$$4 + 2 = 6 < 8$$

$$4 + 3 = 7 < 8$$

$$4 + 4 = 8$$

$$4 + 5 = 9 > 8, \text{ so one of the ordered pairs is } (4, 5)$$

$$5 + 1 = 6 < 8$$

$$5 + 2 = 7 < 8$$

$$5 + 3 = 8$$

$$5 + 4 = 9 > 8, \text{ so one of the ordered pairs is } (5, 4)$$

$$5 + 5 = 10 > 8, \text{ so one of the ordered pairs is } (5, 5)$$

Therefore, the set of ordered pairs satisfying  $x + y > 8 = \{(4, 5), (5, 4), (5, 5)\}$ .

**6. Given  $R = \{(x, y) : x, y \in W, x^2 + y^2 = 25\}$ . Find the domain and Range of R.**

**Solution:**

According to the question,

$$R = \{(x, y) : x, y \in W, x^2 + y^2 = 25\}$$

$$R = \{(0, 5), (3, 4), (4, 3), (5, 0)\}$$

The domain of R consists of all the first elements of all the ordered pairs of R.

$$\text{Domain of } R = \{0, 3, 4, 5\}$$

The range of R contains all the second elements of all the ordered pairs of R.

$$\text{Range of } R = \{5, 4, 3, 0\}$$

**7. If  $R_1 = \{(x, y) \mid y = 2x + 7, \text{ where } x \in R \text{ and } -5 \leq x \leq 5\}$  is a relation. Then find the domain and Range of  $R_1$ .**

**Solution:**

According to the question,

$$R_1 = \{(x, y) \mid y = 2x + 7, \text{ where } x \in R \text{ and } -5 \leq x \leq 5\} \text{ is a relation}$$

The domain of  $R_1$  consists of all the first elements of all the ordered pairs of  $R_1$ , i.e., x,

It is also given  $-5 \leq x \leq 5$ .

Therefore,

$$\text{Domain of } R_1 = [-5, 5]$$

The range of R contains all the second elements of all the ordered pairs of  $R_1$ , i.e., y

$$\text{It is also given } y = 2x + 7$$

$$\text{Now } x \in [-5, 5]$$

Multiply LHS and RHS by 2,

We get,

$$2x \in [-10, 10]$$

Adding LHS and RHS with 7,

We get,



$$2x + 7 \in [-3, 17]$$

$$\text{Or, } y \in [-3, 17]$$

So,

$$\text{Range of } R_1 = [-3, 17]$$

**8. If  $R_2 = \{(x, y) \mid x \text{ and } y \text{ are integers and } x^2 + y^2 = 64\}$  is a relation. Then find  $R_2$ .**

**Solution:**

We have,

$$R_2 = \{(x, y) \mid x \text{ and } y \text{ are integers and } x^2 + y^2 = 64\}$$

So, we get,

$$x^2 = 0 \text{ and } y^2 = 64 \text{ or } x^2 = 64 \text{ and } y^2 = 0$$

$$x = 0 \text{ and } y = \pm 8 \text{ or } x = \pm 8 \text{ and } y = 0$$

$$\text{Therefore, } R_2 = \{(0, 8), (0, -8), (8, 0), (-8, 0)\}$$

**9. If  $R_3 = \{(x, |x|) \mid x \text{ is a real number}\}$  is a relation. Then find domain and range of  $R_3$ .**

**Solution:**

According to the question,

$$R_3 = \{(x, |x|) \mid x \text{ is a real number}\} \text{ is a relation}$$

Domain of  $R_3$  consists of all the first elements of all the ordered pairs of  $R_3$ , i.e.,  $x$ ,

It is also given that  $x$  is a real number,

$$\text{So, Domain of } R_3 = \mathbb{R}$$

Range of  $R$  contains all the second elements of all the ordered pairs of  $R_3$ , i.e.,  $|x|$

It is also given that  $x$  is a real number,

$$\text{So, } |x| = |R|$$

$$\Rightarrow |x| \geq 0,$$

i.e.,  $|x|$  has all positive real numbers including 0

Hence,

$$\text{Range of } R_3 = [0, \infty)$$

**10. Is the given relation a function? Give reasons for your answer.**

(i)  $h = \{(4, 6), (3, 9), (-11, 6), (3, 11)\}$

(ii)  $f = \{(x, x) \mid x \text{ is a real number}\}$

(iii)  $g = n, (1/n) \mid n \text{ is a positive integer}$

(iv)  $s = \{(n, n^2) \mid n \text{ is a positive integer}\}$

(v)  $t = \{(x, 3) \mid x \text{ is a real number}\}$

**Solution:**

(i) According to the question,

$$h = \{(4, 6), (3, 9), (-11, 6), (3, 11)\}$$

Therefore, element 3 has two images, namely, 9 and 11.

A relation is said to be function if every element of one set has one and only one image in other set.

Hence,  $h$  is not a function.

(ii) According to the question,

$$f = \{(x, x) \mid x \text{ is a real number}\}$$

This means the relation  $f$  has elements which are real number.

Therefore, for every  $x \in \mathbb{R}$  there will be unique image.

A relation is said to be function if every element of one set has one and only one image in other set.

Hence,  $f$  is a function.

(iii) According to the question,

$g = n, (1/n) \mid n$  is a positive integer

Therefore, the element  $n$  is a positive integer and the corresponding  $1/n$  will be a unique and distinct number.

Therefore, every element in the domain has unique image.

A relation is said to be function if every element of one set has one and only one image in other set.

Hence,  $g$  is a function.

(iv) According to the question,

$s = \{(n, n^2) \mid n \text{ is a positive integer}\}$

Therefore, element  $n$  is a positive integer and the corresponding  $n^2$  will be a unique and distinct number, as square of any positive integer is unique.

Therefore, every element in the domain has unique image.

A relation is said to be function if every element of one set has one and only one image in other set.

Hence,  $s$  is a function.

(v) According to the question,

$t = \{(x, 3) \mid x \text{ is a real number}\}$

Therefore, the domain element  $x$  is a real number.

Also, range has one number i.e., 3 in it.

Therefore, for every element in the domain has the image 3, it is a constant function.

A relation is said to be function if every element of one set has one and only one image in other set.

Hence,  $t$  is a function.

**11. If  $f$  and  $g$  are real functions defined by  $f(x) = x^2 + 7$  and  $g(x) = 3x + 5$ , find each of the following**

(a)  $f(3) + g(-5)$

(b)  $f(1/2) \times g(14)$

(c)  $f(-2) + g(-1)$

(d)  $f(t) - f(-2)$

(e)  $(f(t) - f(5))/(t - 5)$ , if  $t \neq 5$

**Solution:**

According to the question,

$f$  and  $g$  are real functions such that  $f(x) = x^2 + 7$  and  $g(x) = 3x + 5$

(a)  $f(3) + g(-5)$

$f(x) = x^2 + 7$

Substituting  $x = 3$  in  $f(x)$ , we get

$$f(3) = 3^2 + 7 = 9 + 7 = 16 \dots(i)$$

And,

$$g(x) = 3x + 5$$

Substituting  $x = -5$  in  $g(x)$ , we get

$$g(-5) = 3(-5) + 5 = -15 + 5 = -10 \dots(ii)$$

Adding equations (i) and (ii),

We get,

$$f(3) + g(-5) = 16 - 10 = 6$$

$$(b) f(1/2) \times g(14)$$

$$f(x) = x^2 + 7$$

Substituting  $x = 1/2$  in  $f(x)$ , we get

$$f(1/2) = (1/2)^2 + 7 = 1/4 + 7 = 29/4 \dots(i)$$

And,

$$g(x) = 3x + 5$$

Substituting  $x = 14$  in  $g(x)$ , we get

$$g(14) = 3(14) + 5 = 42 + 5 = 47 \dots(ii)$$

Multiplying equation (i) and (ii),

We get,

$$f(1/2) \times g(14) = (29/4) \times 47 = 1363/4$$

$$(c) f(-2) + g(-1)$$

$$f(x) = x^2 + 7$$

Substituting  $x = -2$  in  $f(x)$ , we get

$$f(-2) = (-2)^2 + 7 = 4 + 7 = 11 \dots(i)$$

And,

$$g(x) = 3x + 5$$

Substituting  $x = -1$  in  $g(x)$ , we get

$$g(-1) = 3(-1) + 5$$

$$= -3 + 5 = 2 \dots(ii)$$

Adding equation (i) and (ii),

We get,

$$f(-2) + g(-1) = 11 + 2 = 13$$

$$(d) f(t) - f(-2)$$

$$f(x) = x^2 + 7$$

Substituting  $x = t$  in  $f(x)$ , we get

$$f(t) = t^2 + 7 \dots(i)$$

Considering the same function,

$$f(x) = x^2 + 7$$

Substituting  $x = -2$  in  $f(x)$ , we get

$$f(-2) = (-2)^2 + 7 = 4 + 7 = 11 \dots(ii)$$

Subtracting equation (i) with (ii),

We get,

$$f(t) - f(-2) = t^2 + 7 - 11 = t^2 - 4$$

(e)  $(f(t) - f(5)) / (t - 5)$ , if  $t \neq 5$

$$f(x) = x^2 + 7$$

Substituting  $x = t$  in  $f(x)$ , we get

$$f(t) = t^2 + 7 \dots\dots\dots(i)$$

Considering the same function,

$$f(x) = x^2 + 7$$

Substituting  $x = 5$  in  $f(x)$ , we get

$$f(5) = (5)^2 + 7 = 25 + 7 = 32 \dots\dots\dots(ii)$$

From equation (i) and (ii), we get

$$\begin{aligned} \frac{f(t) - f(5)}{t - 5} &= \frac{t^2 + 7 - 32}{t - 5} \\ &= \frac{t^2 - 25}{t - 5} \\ &= \frac{t^2 - 5^2}{t - 5} \end{aligned}$$

But we know  $a^2 - b^2 = (a + b)(a - b)$ , so above equation becomes,

$$\frac{f(t) - f(5)}{t - 5} = \frac{(t + 5)(t - 5)}{t - 5}$$

Cancelling the like terms, we get

$$\frac{f(t) - f(5)}{t - 5} = t + 5$$

**12. Let  $f$  and  $g$  be real functions defined by  $f(x) = 2x + 1$  and  $g(x) = 4x - 7$ .**

**(a) For what real numbers  $x$ ,  $f(x) = g(x)$ ?**

**(b) For what real numbers  $x$ ,  $f(x) < g(x)$ ?**

**Solution:**

According to the question,

$f$  and  $g$  be real functions defined by  $f(x) = 2x + 1$  and  $g(x) = 4x - 7$

(a) For what real numbers  $x$ ,  $f(x) = g(x)$

To satisfy the condition  $f(x) = g(x)$ ,

Should also satisfy,

$$2x + 1 = 4x - 7$$

$$\Rightarrow 7 + 1 = 4x - 2x$$

$$\Rightarrow 8 = 2x$$

$$\text{Or, } 2x = 8$$

$$\Rightarrow x = 4$$

Hence, we get,

$$\text{For } x = 4, f(x) = g(x)$$

(b) For what real numbers  $x$ ,  $f(x) < g(x)$

To satisfy the condition  $f(x) < g(x)$ ,

Should also satisfy,

$$2x + 1 < 4x - 7$$



$$\Rightarrow 7 + 1 < 4x - 2x$$

$$\Rightarrow 8 < 2x$$

$$\text{Or, } 2x > 8$$

$$\Rightarrow x > 4$$

Hence, we get,

$$\text{For } x > 4, f(x) > g(x)$$

**13. If  $f$  and  $g$  are two real valued functions defined as  $f(x) = 2x + 1$ ,  $g(x) = x^2 + 1$ , then find.**

**(i)  $f + g$  (ii)  $f - g$  (iii)  $fg$  (iv)  $f/g$**

**Solution:**

According to the question,

$f$  and  $g$  be real valued functions defined as  $f(x) = 2x + 1$ ,  $g(x) = x^2 + 1$ ,

(i)  $f + g$

$$\begin{aligned}\Rightarrow f + g &= f(x) + g(x) \\ &= 2x + 1 + x^2 + 1 \\ &= x^2 + 2x + 2\end{aligned}$$

(ii)  $f - g$

$$\begin{aligned}\Rightarrow f - g &= f(x) - g(x) \\ &= 2x + 1 - (x^2 + 1) \\ &= 2x - x^2\end{aligned}$$

(iii)  $fg$

$$\begin{aligned}\Rightarrow fg &= f(x) g(x) \\ &= (2x + 1)(x^2 + 1) \\ &= 2x(x^2) + 2x(1) + 1(x^2) + 1(1) \\ &= 2x^3 + 2x + x^2 + 1 \\ &= 2x^3 + x^2 + 2x + 1\end{aligned}$$

(iv)  $f/g$

$$f/g = f(x)/g(x)$$

$$\Rightarrow \frac{f}{g} = \frac{(2x + 1)}{x^2 + 1}$$

**14. Express the following functions as set of ordered pairs and determine their range.**

**$f: X \rightarrow R, f(x) = x^3 + 1$ , where  $X = \{-1, 0, 3, 9, 7\}$**

**Solution:**

According to the question,

A function  $f: X \rightarrow R, f(x) = x^3 + 1$ , where  $X = \{-1, 0, 3, 9, 7\}$

Domain =  $f$  is a function such that the first elements of all the ordered pair belong to the set  $X = \{-1, 0, 3, 9, 7\}$ .

The second element of all the ordered pair are such that they satisfy the condition  $f(x) = x^3 + 1$

When  $x = -1$ ,

$$f(x) = x^3 + 1$$

$$f(-1) = (-1)^3 + 1 = -1 + 1 = 0 \Rightarrow \text{ordered pair} = (-1, 0)$$

When  $x = 0$ ,  
 $f(x) = x^3 + 1$   
 $f(0) = (0)^3 + 1 = 0 + 1 = 1 \Rightarrow$  ordered pair  $= (0, 1)$   
 When  $x = 3$ ,  
 $f(x) = x^3 + 1$   
 $f(3) = (3)^3 + 1 = 27 + 1 = 28 \Rightarrow$  ordered pair  $= (3, 28)$   
 When  $x = 9$ ,  
 $f(x) = x^3 + 1$   
 $f(9) = (9)^3 + 1 = 729 + 1 = 730 \Rightarrow$  ordered pair  $= (9, 730)$   
 When  $x = 7$ ,  
 $f(x) = x^3 + 1$   
 $f(7) = (7)^3 + 1 = 343 + 1 = 344 \Rightarrow$  ordered pair  $= (7, 344)$   
 Therefore, the given function as a set of ordered pairs is  
 $f = \{(-1, 0), (0, 1), (3, 28), (7, 344), (9, 730)\}$   
 And,  
 Range of  $f = \{0, 1, 28, 730, 344\}$

**15. Find the values of  $x$  for which the functions  $f(x) = 3x^2 - 1$  and  $g(x) = 3 + x$  are equal**

**Solution:**

According to the question,  
 $f$  and  $g$  functions defined by  $f(x) = 3x^2 - 1$  and  $g(x) = 3 + x$   
 For what real numbers  $x$ ,  $f(x) = g(x)$   
 To satisfy the condition  $f(x) = g(x)$ ,  
 Should also satisfy,  
 $3x^2 - 1 = 3 + x$   
 $\Rightarrow 3x^2 - x - 3 - 1 = 0$   
 $\Rightarrow 3x^2 - x - 4 = 0$   
 Splitting the middle term,  
 We get,  
 $\Rightarrow 3x^2 + 3x - 4x - 4 = 0$   
 $\Rightarrow 3x(x + 1) - 4(x + 1) = 0$   
 $\Rightarrow (3x - 4)(x + 1) = 0$   
 $\Rightarrow 3x - 4 = 0$  or  $x + 1 = 0$   
 $\Rightarrow 3x = 4$  or  $x = -1$   
 $\Rightarrow x = 4/3, -1$   
 Hence, for  $x = 4/3, -1$ ,  $f(x) = g(x)$ ,  
 i.e., given functions are equal.

### LONG ANSWER TYPE

**16. Is  $g = \{(1, 1), (2, 3), (3, 5), (4, 7)\}$  a function? Justify. If this is described by the relation,  $g(x) = \alpha x + \beta$ , then what values should be assigned to  $\alpha$  and  $\beta$ ?**

**Solution:**

According to the question,  
 $g = \{(1, 1), (2, 3), (3, 5), (4, 7)\}$ , and is described by relation  $g(x) = \alpha x + \beta$

Now, given the relation,

$$g = \{(1, 1), (2, 3), (3, 5), (4, 7)\}$$

$$g(x) = \alpha x + \beta$$

For ordered pair (1,1),  $g(x) = \alpha x + \beta$ , becomes

$$g(1) = \alpha(1) + \beta = 1$$

$$\Rightarrow \alpha + \beta = 1$$

$$\Rightarrow \alpha = 1 - \beta \dots(i)$$

Considering ordered pair (2, 3),  $g(x) = \alpha x + \beta$ , becomes

$$g(2) = \alpha(2) + \beta = 3$$

$$\Rightarrow 2\alpha + \beta = 3$$

Substituting value of  $\alpha$  from equation (i), we get

$$\Rightarrow 2(2) + \beta = 3$$

$$\Rightarrow \beta = 3 - 4 = -1$$

Substituting value of  $\beta$  in equation (i), we get

$$\alpha = 1 - \beta = 1 - (-1) = 2$$

Now, the given equation becomes,

$$\text{i.e., } g(x) = 2x - 1$$

**17. Find the domain of each of the following functions given by**

$$(i) \quad f(x) = \frac{1}{\sqrt{1 - \cos x}}$$

$$(ii) \quad f(x) = \frac{1}{\sqrt{x + |x|}}$$

$$(iii) \quad f(x) = x |x|$$

$$(iv) \quad f(x) = \frac{x^3 - x + 3}{x^2 - 1}$$

$$(v) \quad f(x) = \frac{3x}{2x - 8}$$

**Solution:**

(i)

$$f(x) = \frac{1}{\sqrt{1 - \cos x}}$$

According to the question,

We know the value of  $\cos x$  lies between  $-1, 1$ ,

$$-1 \leq \cos x \leq 1$$

Multiplying by negative sign, we get

$$\text{Or } 1 \geq -\cos x \geq -1$$

Adding 1, we get

$$2 \geq 1 - \cos x \geq 0 \dots(i)$$

Now,

$$f(x) = \frac{1}{\sqrt{1-\cos x}},$$

$$1 - \cos x \neq 0$$

$$\Rightarrow \cos x \neq 1$$

$$\text{Or, } x \neq 2n\pi \forall n \in \mathbb{Z}$$

Therefore, the domain of  $f = \mathbb{R} - \{2n\pi : n \in \mathbb{Z}\}$

(ii)

$$f(x) = \frac{1}{\sqrt{x + |x|}}$$

According to the question,

For real value of  $f$ ,

$$x + |x| > 0$$

When  $x > 0$ ,

$$x + |x| > 0 \Rightarrow x + x > 0 \Rightarrow 2x > 0 \Rightarrow x > 0$$

When  $x < 0$ ,

$$x + |x| > 0 \Rightarrow x - x > 0 \Rightarrow 2x > 0 \Rightarrow x > 0$$

So,  $x > 0$ , to satisfy the given equation.

Therefore, the domain of  $f = \mathbb{R}^+$

(iii)

$$f(x) = x|x|$$

According to the question,

We know  $x$  and  $|x|$  are defined for all real values.

Therefore, the domain of  $f = \mathbb{R}$

(iv)

$$f(x) = \frac{(x^3 - x + 3)}{x^2 - 1}$$

According to the question,

For real value of

$$x^2 - 1 \neq 0$$

$$\Rightarrow (x-1)(x+1) \neq 0$$

$$\Rightarrow x-1 \neq 0 \text{ or } x+1 \neq 0$$

$$\Rightarrow x \neq 1 \text{ or } x \neq -1$$

Therefore, the domain of  $f = \mathbb{R} - \{-1, 1\}$

(v)

$$f(x) = \frac{3x}{2x-8}$$

According to the question,

For real value of

$$2x - 8 \neq 0$$

$$\Rightarrow x \neq 4$$



Therefore, the domain of  $f = \mathbb{R} - \{28\}$

**18. Find the range of the following functions given by**

(i)  $f(x) = \frac{3}{2-x^2}$

(ii)  $f(x) = 1 - |x-2|$

(iii)  $f(x) = |x-3|$

(iv)  $f(x) = 1 + 3 \cos 2x$

**Solution:**

(i)

$$f(x) = \frac{3}{2-x^2}$$

According to the question,

Let  $f(x) = y$ ,

$$y = \frac{3}{2-x^2}$$

$$\Rightarrow 2-x^2 = \frac{3}{y}$$

$$\Rightarrow x^2 = 2 - \frac{3}{y}$$

But, we know that,  $x^2 \geq 0$

$$2 - \frac{3}{y} \geq 0$$

$$\Rightarrow \frac{2y-3}{y} \geq 0$$

$$\Rightarrow y > 0 \text{ and } 2y-3 \geq 0$$

$$\Rightarrow y > 0 \text{ and } 2y \geq 3$$

$$\Rightarrow y > 0 \text{ and } y \geq \frac{3}{2}$$

Or  $f(x) > 0$  and  $f(x) \geq \frac{3}{2}$

$$f(x) \in (-\infty, 0) \cup \left[\frac{3}{2}, \infty\right)$$

$$\Rightarrow f(x) \in (-\infty, 0) \cup \left[\frac{3}{2}, \infty\right)$$

Therefore, the range of  $f = (-\infty, 0) \cup \left[\frac{3}{2}, \infty\right)$

(ii)  $f(x) = 1 - |x-2|$

According to the question,

For real value of  $f$ ,

$$|x-2| \geq 0$$

Adding negative sign, we get

$$\text{Or } -|x-2| \leq 0$$

Adding 1 we get

$$\Rightarrow 1 - |x-2| \leq 1$$

$$\text{Or } f(x) \leq 1$$

$$\Rightarrow f(x) \in (-\infty, 1]$$

Therefore, the range of  $f = (-\infty, 1]$

$$(iii) f(x) = |x-3|$$

According to the question,

We know  $|x|$  are defined for all real values.

And  $|x-3|$  will always be greater than or equal to 0.

$$\text{i.e., } f(x) \geq 0$$

Therefore, the range of  $f = [0, \infty)$

$$(iv) f(x) = 1 + 3 \cos 2x$$

According to the question,

We know the value of  $\cos 2x$  lies between  $-1, 1$ , so

$$-1 \leq \cos 2x \leq 1$$

Multiplying by 3, we get

$$-3 \leq 3 \cos 2x \leq 3$$

Adding 1, we get

$$-2 \leq 1 + 3 \cos 2x \leq 4$$

$$\text{Or, } -2 \leq f(x) \leq 4$$

$$\text{Hence } f(x) \in [-2, 4]$$

Therefore, the range of  $f = [-2, 4]$

**19. Redefine the function  $f(x) = |x-2| + |2+x|$ ,  $-3 \leq x \leq 3$**

**Solution:**

According to the question,

$$\text{function } f(x) = |x-2| + |2+x|, -3 \leq x \leq 3$$

We know that,

when  $x > 0$ ,

$$|x-2| \text{ is } (x-2), x \geq 2$$

$$|2+x| \text{ is } (2+x), x \geq -2$$

when  $x < 0$

$$|x-2| \text{ is } -(x-2), x < 2$$

$$|2+x| \text{ is } -(2+x), x < -2$$

$$\text{Given that, } f(x) = |x-2| + |2+x|, -3 \leq x \leq 3$$

It can be rewritten as,

$$f(x) = \begin{cases} -(x-2) - (2+x), & -3 \leq x < -2 \\ -(x-2) + (2+x), & -2 \leq x < 2 \\ (x-2) + (2+x), & 2 \leq x \leq 3 \end{cases}$$

Or

$$f(x) = \begin{cases} -x + 2 - 2 - x, & -3 \leq x < -2 \\ -x + 2 + 2 + x, & -2 \leq x < 2 \\ x - 2 + 2 + x, & 2 \leq x \leq 3 \end{cases}$$

Or,

$$f(x) = \begin{cases} -2x, & -3 \leq x < -2 \\ 4, & -2 \leq x < 2 \\ 2x, & 2 \leq x \leq 3 \end{cases}$$

20. If

$$f(x) = \frac{x-1}{x+1}, \text{ then show that:}$$

$$(i) \quad f\left(\frac{1}{x}\right) = -f(x)$$

$$(ii) \quad f\left(-\frac{1}{x}\right) = \frac{-1}{f(x)}$$

**Solution:**

(i)

$$f(x) = \frac{x-1}{x+1}$$

Substituting x by 1/x, we get

$$f\left(\frac{1}{x}\right) = \frac{\frac{1}{x}-1}{\frac{1}{x}+1}$$

$$= \frac{\frac{1-x}{x}}{\frac{1+x}{x}}$$

$$= \frac{1-x}{1+x}$$

$$= \frac{-(x-1)}{1+x}$$

$$= -\frac{x-1}{x+1}$$

Therefore,

We get,

$$f\left(\frac{1}{x}\right) = -f(x)$$

Hence proved

(ii)

$$f(x) = \frac{x-1}{x+1}$$

Substituting x by -1/x, we get

$$f\left(-\frac{1}{x}\right) = \frac{\left(-\frac{1}{x}\right) - 1}{\left(-\frac{1}{x}\right) + 1}$$

$$= \frac{\frac{-1-x}{x}}{\frac{-1+x}{x}}$$

$$= \frac{-1-x}{-1+x}$$

$$= \frac{x-1}{x+1}$$

$$\text{Therefore, } f\left(-\frac{1}{x}\right) = \frac{-1}{f(x)}$$

Hence proved

**21. Let  $f(x) = \sqrt{x}$  and  $g(x) = x$  be two functions defined in the domain  $\mathbb{R}^+ \cup \{0\}$ . Find**

**(i)  $(f + g)(x)$**

**(ii)  $(f - g)(x)$**

**(iii)  $(fg)(x)$**

**(iv)  $(f/g)(x)$**

**Solution:**

(i)

$$(f + g)(x)$$

$$\Rightarrow (f + g)(x) = f(x) + g(x)$$

$$\Rightarrow f(x) + g(x) = \sqrt{x} + x$$

(ii)

$$(f - g)(x)$$

$$\Rightarrow (f - g)(x) = f(x) - g(x)$$

$$\Rightarrow f(x) - g(x) = \sqrt{x} - x$$

(iii)

$$(fg)(x)$$

$$\Rightarrow (fg)(x) = f(x) \cdot g(x)$$

$$\Rightarrow (fg)(x) = (\sqrt{x})(x)$$

$$\Rightarrow f(x)g(x) = x\sqrt{x}$$

(iv)

$$(f/g)(x) = f(x)/g(x)$$



$$\Rightarrow \left(\frac{f}{g}\right)(x) = \frac{\sqrt{x}}{x}$$

Multiplying and dividing by  $\sqrt{x}$ ,

We get

$$= \frac{\sqrt{x}}{x} \times \frac{\sqrt{x}}{\sqrt{x}}$$

$$= \frac{x}{x\sqrt{x}}$$

$$\Rightarrow \left(\frac{f}{g}\right)(x) = \frac{1}{\sqrt{x}}$$



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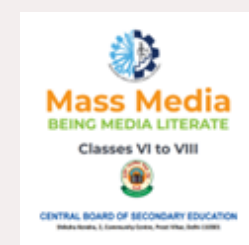
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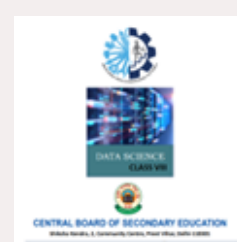
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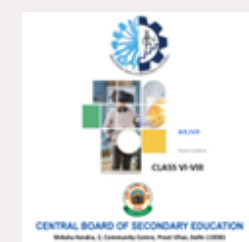
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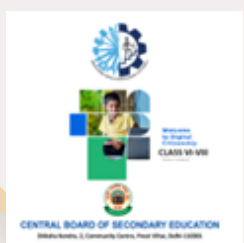
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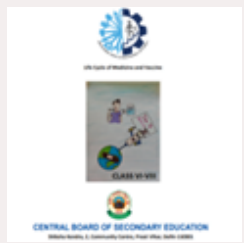
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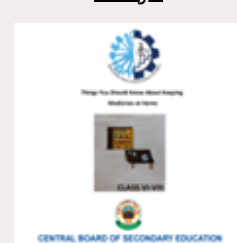
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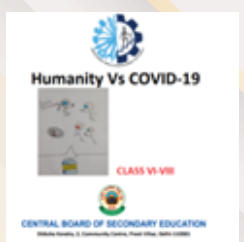
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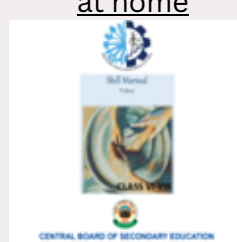
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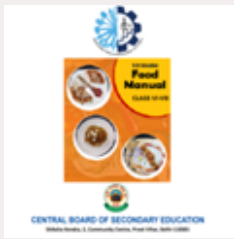
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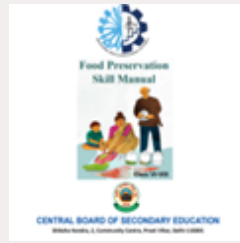
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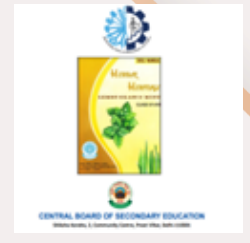
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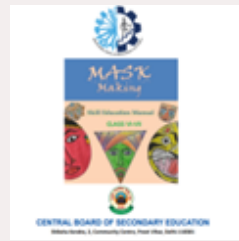
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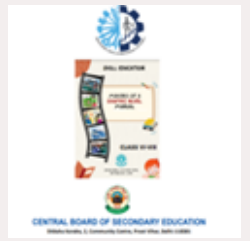
Khadi



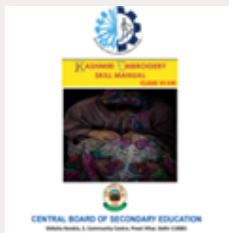
Mask Making



Mass Media



Making of a Graphic Novel



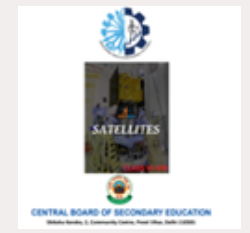
Kashmiri Embroidery



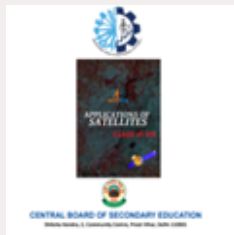
Embroidery



Rockets



Satellites



Application of Satellites

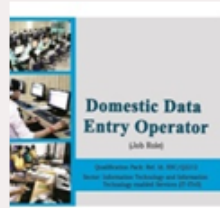


Photography

# SKILL SUBJECTS AT SECONDARY LEVEL (CLASSES IX – X)



Retail



Information Technology



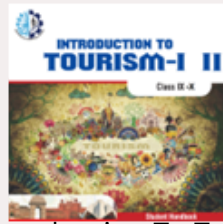
Security



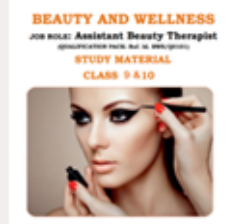
Automotive



Introduction To Financial Markets



Introduction To Tourism



Beauty & Wellness



Agriculture



Food Production



Front Office Operations



Banking & Insurance



Marketing & Sales



Health Care



Apparel



Multi Media



Multi Skill Foundation Course



Artificial Intelligence



Physical Activity Trainer



Data Science



Electronics & Hardware (NEW)



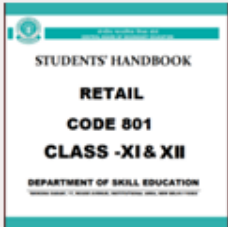
Foundation Skills For Sciences (Pharmaceutical & Biotechnology)(NEW)



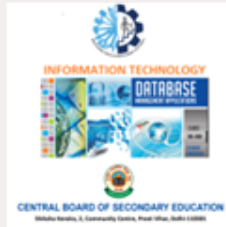
Design Thinking & Innovation (NEW)



# SKILL SUBJECTS AT SR. SEC. LEVEL (CLASSES XI – XII)



Retail



Information Technology



Web Application



Automotive



Financial Markets Management



Tourism



Beauty & Wellness



Agriculture



Food Production



Front Office Operations



Banking



Marketing



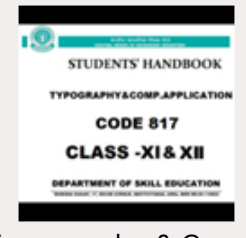
Health Care



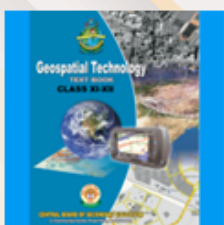
Insurance



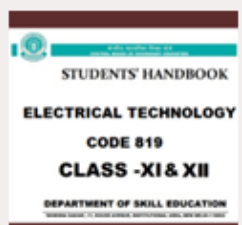
Horticulture



Typography & Comp.  
Application



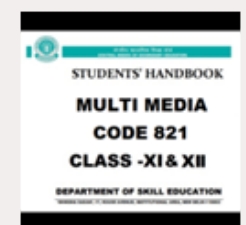
Geospatial Technology



Electrical Technology



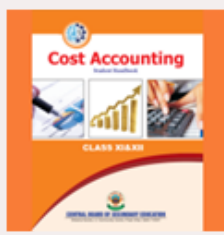
Electronic Technology



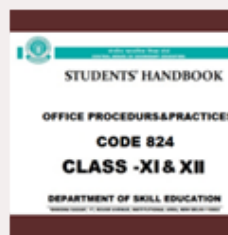
Multi-Media



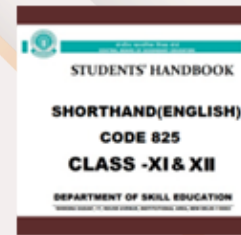
Taxation



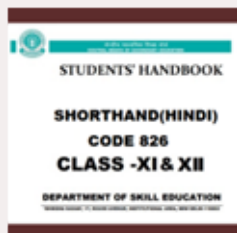
Cost Accounting



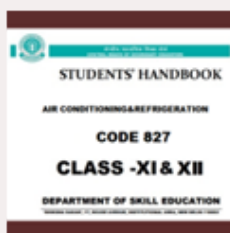
Office Procedures & Practices



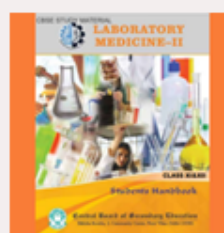
Shorthand (English)



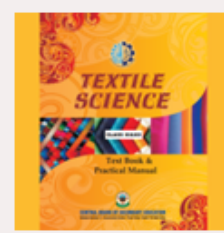
Shorthand (Hindi)



Air-Conditioning & Refrigeration



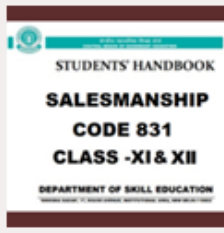
Medical Diagnostics



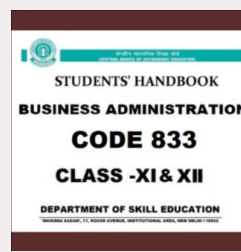
Textile Design



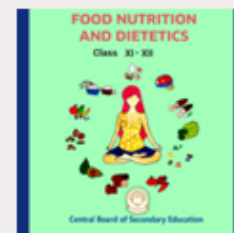
Design



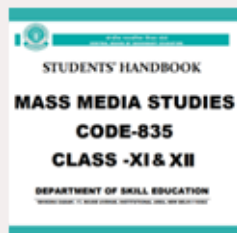
Salesmanship



Business Administration



Food Nutrition & Dietetics



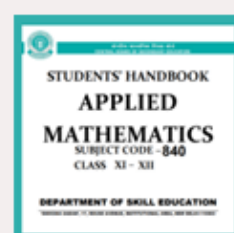
Mass Media Studies



Library & Information Science



Fashion Studies



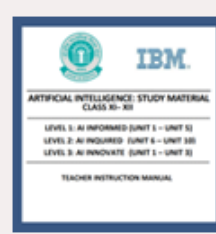
Applied Mathematics



Yoga



Early Childhood Care & Education



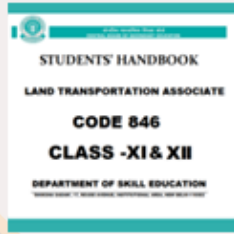
Artificial Intelligence



Data Science



Physical Activity Trainer(new)



Land Transportation Associate (NEW)



Electronics & Hardware (NEW)



Design Thinking & Innovation (NEW)